

**From:** [Robinson, Angela Y. \(Fed\)](#)  
**To:** [Moody, Dustin \(Fed\)](#)  
**Cc:** [Perlner, Ray A. \(Fed\)](#); [Alperin-Sheriff, Jacob \(Fed\)](#)  
**Subject:** Re: Round 5 spec  
**Date:** Friday, April 26, 2019 2:52:32 PM

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Please clarify some details of Algorithm 1 related to the creation of S and B. We believe a paragraph about deterministic function  $f_S$  would be helpful to include in section 2.4.3, similar to that of deterministic function  $f_R$ . We are also trying to reconcile the creation of B, using the rounding function as defined in section 2.2, in both the ring and non-ring cases.

We referred to section 2.11.6, core function "create\_S\_T" for more information. The description of this core function states that dimension of  $S^T$  is  $\bar{n} \times d$ , so the dimensions of S are  $d \times \bar{n}$ . In the ring case, it seems that B is created by taking the matrix product AS, reducing each entry mod  $\Phi_{n+1}$ , then adding rational number  $h_1$ . Please clarify what is meant by the sum of a matrix with  $h_1$ . In the non-ring case, does  $S^T$  still have dimensions  $\bar{n} \times d$ ?

Thanks,  
Angela

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**From:** Moody, Dustin (Fed)  
**Sent:** Friday, April 26, 2019 6:36:07 AM  
**To:** Robinson, Angela Y. (Fed)  
**Cc:** Perlner, Ray (Fed); Alperin-Sheriff, Jacob (Fed)  
**Subject:** Re: Round 5 spec

Angela,

Sounds good. Can you write up a request to the Round 5 team, and then bounce it around Ray, Jacob, Daniel(s), and I? Then we'll send it to Round5. Thanks,

Dustin

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**From:** Robinson, Angela Y. (Fed)  
**Sent:** Thursday, April 25, 2019 2:30 PM  
**To:** Moody, Dustin (Fed)  
**Cc:** Perlner, Ray (Fed); Alperin-Sheriff, Jacob (Fed)  
**Subject:** Round 5 spec

Hi Dustin,

More clarification is needed from the Round5 team on details relating to section 2.4.3 Algorithm 1, step 5. The process to generate B is not clear.

A is either a  $d \times d$  square matrix (in the non-Ring case) or A is a single polynomial (in the Ring case). In either case, A is multiplied by S. We request some information about the deterministic function  $f_S$ , similar to the paragraph found in section 2.4.3 about the deterministic function  $f_R$ . This information should include the dimensions of the output S.

The rounding function  $R_{\{a \rightarrow b, h\}}$  is defined explicitly in section 2.2. By this definition, Algorithm 1, step 5 includes some operation of the form  $\langle AS \rangle_{\Phi + h_1}$ . Because we do not know the dimensions of S, it is not clear whether AS will be a vector or a matrix, but in either case it is not clear how to add  $h_1$  to AS. In the case that AS is a square matrix, does this mean to add  $h_1 * \text{Identity}$ ?

I talked to Ray and Jacob and they agree that more clarification is needed, but maybe this request should be ironed out before sending to the team?

Thanks,  
Angela